

# How Should Entrainment be Parameterized?

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$$A_R \neq 0.2$$

(well, hardly ever)

## Definitions:

We're talking about entrainment at the top of convective boundary layers without active moist convection.

Emphasis is on buoyancy flux, but some concepts apply to scalars, moisture, etc. as well.

$$A_R = -\frac{\overline{(w'\theta'_v)_i}}{\overline{(w'\theta'_v)_0}}$$

## What controls entrainment?

- Impinging thermals
- Inversion characteristics (strength and depth)
- Shear across the inversion

The simple notion of an entrainment flux ratio only addresses the first of these.

Effects of inversion characteristics seem to be highly non-linear.

## Issues

**Simple parameterizations underestimate entrainment at the top of convective boundary layers.**

The underestimation is worse when:

- Convection is weaker
- Inversion is weaker
- Shear is stronger

**Pure surface-driven free convection is rare (in a global sense, at least).**

The mixed layer is often in free convection, but the entrainment zone rarely is.

**A ratio can definitely not be applied to potential temperature, moisture, or any other quantity. Only virtual potential temperature can be used with any sort of ratio argument!**

**LES, theory, laboratory experiments, and observations are thought to disagree about how much entrainment occurs.**

Observations show large entrainment ( $A \sim 0.4-0.5$ ) even in cases that might be thought of as free-convective.

LES with finer resolution seem to show a bigger influence of shear.

Tank experiments were at fairly low Reynolds number, and may not represent entrainment structure correctly.

Theoretical expressions for influence of shear give very different results.

**Entrainment dominates the morning transition and is at least 20% of the heat budget at all times.**

The entrainment ratio has a very large magnitude during the early phases of transition.

## Suggestions for improvement:

TKE schemes can handle weakly convective and transitional BLs without "switches," but fine vertical resolution may be necessary.

Entrainment flux can be parameterized as a function of surface flux and entrainment zone Richardson number.

$$R_{ibEZ} = \frac{g(\Delta\theta_v/\theta_{v0})d_{EZ}}{\Delta u_i^2}$$

## Stratification by Entrainment Zone Richardson Number (from Angevine 1999)

	$R_{ibEZ} < 0.5$	$0.5 < R_{ibEZ} < 1.5$	$R_{ibEZ} > 1.5$
$A_R$	$0.86 \pm 0.18$ (0.92)	$0.28 \pm 0.20$ (0.35)	$0.32 \pm 0.19$ (0.20)
$N$ , hours	28	29	34

## (A few) References:

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